

② (a) Water: hydrogen bond strength  $5-8 kT$  ( $\text{@ } 25^\circ\text{C}$ )

on average, 2 H-bonds per molecule of liquid water

(could be  
some discussion  
about this.)

wikipedia gives  
 $\sim 3.24 \text{ @ } 100^\circ\text{C}$ ,  
 $3.59 \text{ @ } 25^\circ\text{C}$   
but also  $2.35 \text{ @ } 25^\circ\text{C}$

$$\text{@ } 25^\circ\text{C}, k_B T \approx (298 \text{ K}) / (1.38 \times 10^{-23} \frac{\text{J}}{\text{K}}) / (6.02 \times 10^{23} \frac{\text{bonds}}{\text{mole}})$$
$$= 2477 \frac{\text{J}}{\text{mole}} \approx 2.5 \text{ kJ/mole}$$

$$\text{@ } 100^\circ\text{C}, k_B T = (373 \text{ K}) / (1.38 \times 10^{-23} \frac{\text{J}}{\text{K}}) / (6.02 \times 10^{23} \frac{\text{bonds}}{\text{mole}})$$
$$= 3100 \frac{\text{J}}{\text{mole}} = 3.1 \text{ kJ/mole}$$

so: H-bond ~~short~~ strength  $\approx 5-8 kT_{25^\circ} \approx 13-20 \text{ kJ/mole}$   
per bond  
for a single bond

If use 2.35 bonds/molecule, it's  $31-47 \text{ kJ/mole}$   
using 3.2 bonds/molecule, it's  $42-64 \text{ kJ/mole}$

Calculated heat of vaporization of water is  
 $40.65 \text{ kJ/mole}$ , so

clearly breaking H-bonds is a large contribution  
to the heat of vaporization of water

(b) Energy of 2 electrons separated by dist.  $r$ :

$$V = \frac{1}{4\pi\epsilon_0} \frac{e^2}{r^2} \quad \text{want } V = k_B T$$

$$\downarrow$$
$$e = KE_0$$
$$k = 80$$

$$\text{so: } k_B T = \frac{1}{4\pi\epsilon_0} \frac{e^2}{r^2}$$

$$r^2 = \frac{(4\pi\epsilon_0)(k_B T)}{e^2}$$

$$\text{for } T = 25^\circ\text{C}, \rightarrow r^2 \approx (0.7 \text{ nm})^2$$