

Solutions to PS # 7

1. $C = q^2 + wq$ $MC = 2q + w$

a. $w = 10$ $C = q^2 + 10q$
 $MC = 2q + 10 = P$ $q = 0.5P - 5$

Industry $Q = \sum_I^{1000} q = 500P - 5000$

at 20, $Q = 5000$; at 21, $Q = 5500$

b. Here, $MC = 2q + .002Q$ for profit maximum, set $= P$

$q = 0.5P - 0.001Q$

Total $Q = \sum_I^{1000} q = 500P - Q$ $Q = 250P$

$P = 20, Q = 5000$
 where

Supply is more steeply sloped in this case

Expanded output bids up wages.

$P = 21, Q = 5250$

2. a. The long-run equilibrium price is $10 + r = 10 + .002Q$.

So, $Q = 1050 \sim 50(10 + .002Q) = 550 - .1Q$ so

$Q = 500, P = 11, r = 1$.

b. Now $Q = 1600 \sim 50(10 + .002Q) = 1100 - .1Q$

$Q = 1000, P = 12, r = 2$.

c. Change in $PS = 1(500) + .5(1)(500) = 750$.

d. Change in rents $= 1(500) + .5(1)(500) = 750$. The areas are equal.

e. With tax $P_D = P_S + 5.5$

$$P_S = 10 + .002Q$$

$$P_D = 15.5 + .002Q$$

$$Q = 1050 - 50(15.5 + .002Q) = 275 - .1Q$$

$$1.1Q = 275 \quad Q = 250 \quad P_D = 16 \quad r = 0.5$$

$$\text{Total tax} = 5.5(250) = 1,375$$

$$\text{Demanders pay } 250(16 - 11) = 1,250$$

$$\text{Producers pay } 250(11 - 10.5) = 125$$

f. $CS \text{ originally} = .5(500)(21 - 11) = 2,500$

$$CS \text{ now} = .5(250)(21 - 16) = 625$$

$$PS \text{ originally} = .5(500)(11 - 10) = 250$$

$$PS \text{ now} = .5(250)(10.5 - 10) = 62.5$$

g. $\text{Loss of rents} = .5(250) + .5(250)(.5) = 187.5$

This is the total loss of PS in part b. Occurs because the only reason for upward sloping supply is upward slope of film royalties supply.

3. The Ramsey formula for optimal taxation

a. Use the deadweight loss formula from Problem 12.9:

$$L = \sum_{i=1}^n DW(t_i) + \lambda \left(T - \sum_{i=1}^n t_i p_i x_i \right)$$

$$\partial L / \partial t_i = .5[e_D e_S / (e_S - e_D)] 2 t_i p_i x_i - \lambda p_i x_i = 0$$

$$\partial L / \partial \lambda = T - \sum_{i=1}^n t_i p_i x_i = 0$$

$$\text{Thus } t_i = -\lambda(e_S - e_D) / e_S e_D = \lambda(1/e_S - 1/e_D)$$

b. The above formula suggests that higher taxes should be applied to goods with more inelastic supply and demand. A tax on a good discourages the consumption and production of that good. Thus, taxing a good with more inelastic supply and demand would result in less change in the consumption of the good. Therefore, the tax would produce smaller distortions: the DWL would be smaller.

c. This result was obtained under a set of very restrictive assumptions. First, it was obtained under partial equilibrium (the welfare analysis is undertaken in each market separately), ignoring the general equilibrium interactions between markets. Also, income effects and cross-price elasticities are not taken into account.

4. a. Long-run equilibrium requires $P = AC = MC$.

$$AC = \frac{k}{q} + a + bq = MC = a + 2bq \quad \text{Hence} \quad q = \sqrt{\frac{k}{b}} \quad P = a + 2\sqrt{kb}$$

b. Want supply = demand $nq = n\sqrt{\frac{k}{b}} = A - BP = A - B(a + 2\sqrt{kb})$

$$\text{Hence, } n = \frac{A - B(a + \sqrt{kb})}{\sqrt{k/b}}.$$

c. Apparently A has a definitely positive effect on n . That makes sense since A reflects the “size” of the market. If $a > 0$, the effect of B on n is clearly negative.

d. It appears that fixed costs (k) have a negative effect on n . The effect of a is also negative (assuming it is a positive constant). The effect of b also seems to be negative. These results make sense. The first shows how greater fixed costs increase the typical firm’s optimal size. The second and third show how higher marginal costs raise price and therefore reduce the number of firms.