

**Problem Set # 6**

**Due 10/26/09**

1. Text Problem 10.5.
2. Text Problem 10.8.
3. Text Problem 10.11 (Hint: Notice that the elasticities of substitution are defined with logarithms)

Note: You should also check how these results work in the Translog Cost Function in the Extensions to chapter 10. A Translog application will be featured in the second examination in this course.

4. Consider the two elementary production functions:

1. Fixed proportions:  $q = [\text{Min}(k, l)]^s$  .
2. Perfect substitutes:  $q = (k + l)^s$

- a. Explain why the parameter  $s$  ( $> 0$ ) measures the returns to scale in each of these production functions.
- b. Calculate the total cost function for each of these production functions.
- c. A total cost function is said to be “separable” if it can be written as

$$C(q, v, w) = f(q) \cdot C(1, v, w)$$

That is, scale effects can be separated from the “unit cost” function.

Are the total cost functions estimated in part b separable? Explain.

- d. Explain how average and marginal cost functions can always be easily derived from separable cost functions. Make that calculation for the two cost functions in part b.