

Before Lab This Week

- Read through the entirety of Lab 6 - RLC Circuits in the manual.
- Pay special attention to all of Section 6.1.
- Do Exercises 1 and 2 and bring these with you to lab.



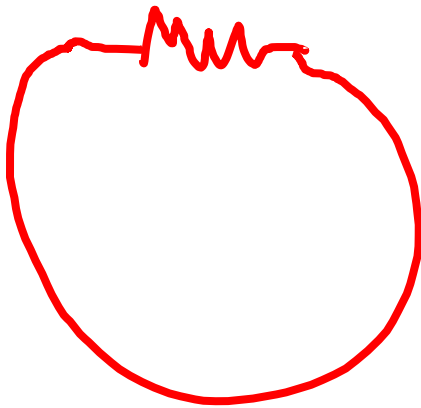
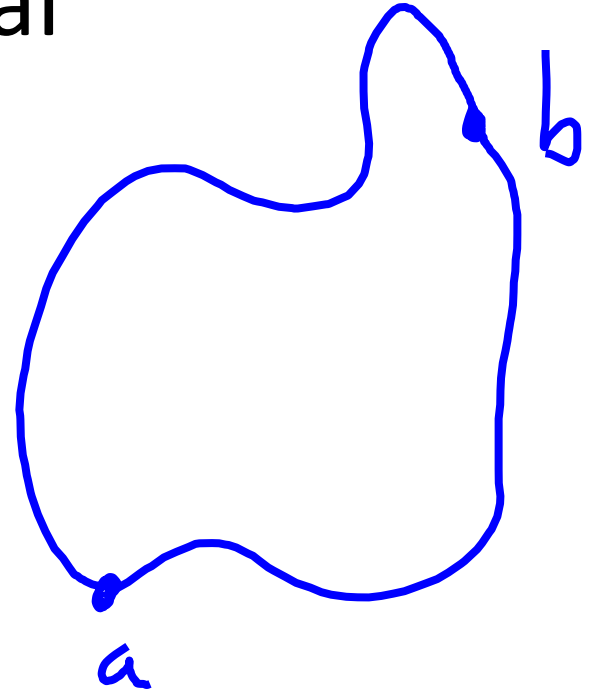
M.C. Escher, Waterfall

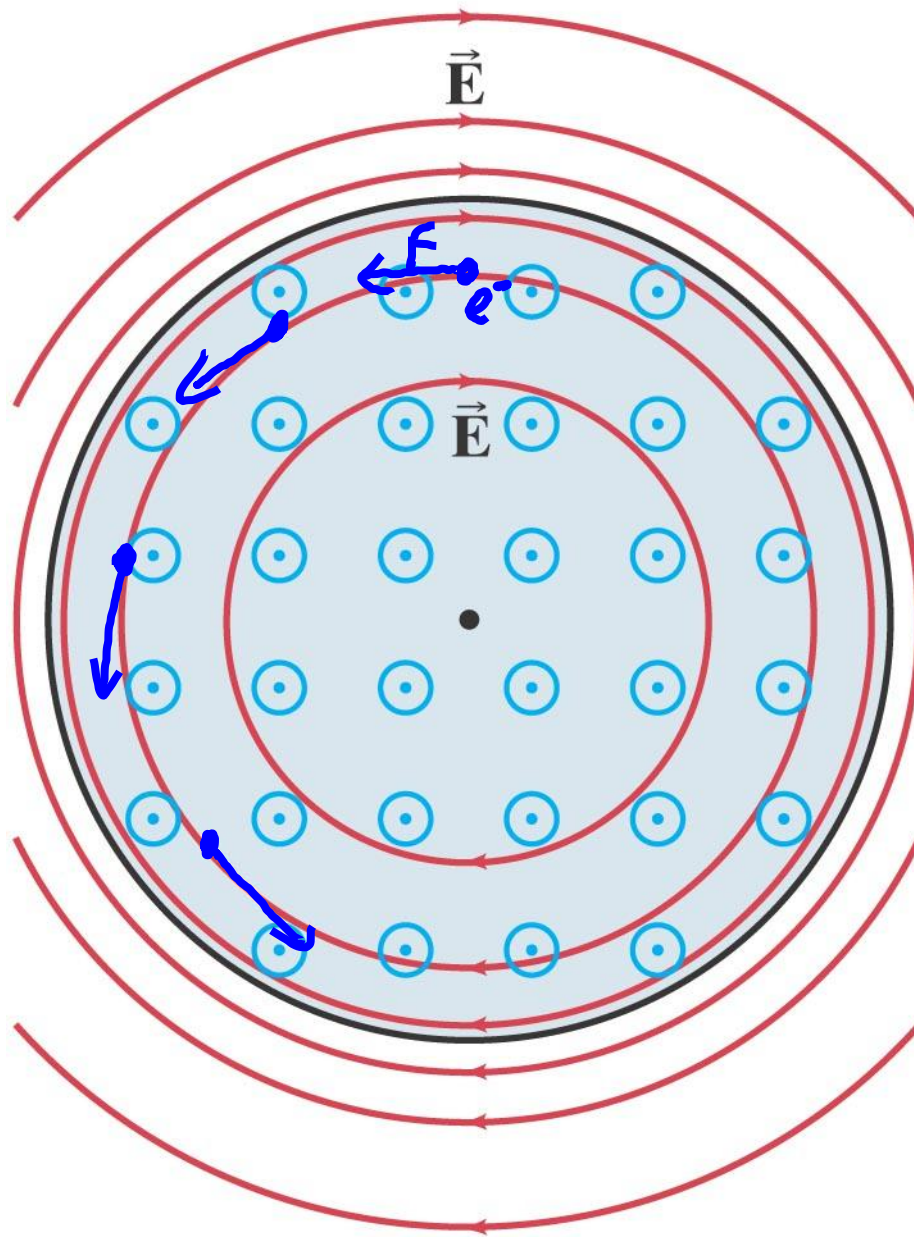
http://en.wikipedia.org/wiki/Waterfall_%28M._C._Escher%29

Electric Potential

$$V_b - V_a = \Delta V = - \int_a^b \vec{E} \cdot d\vec{l}$$

$$\oint \vec{E} \cdot d\vec{l} = 0$$





$$\oint \vec{E} \cdot d\vec{l} \neq 0$$

(c)

Figure 29.27c

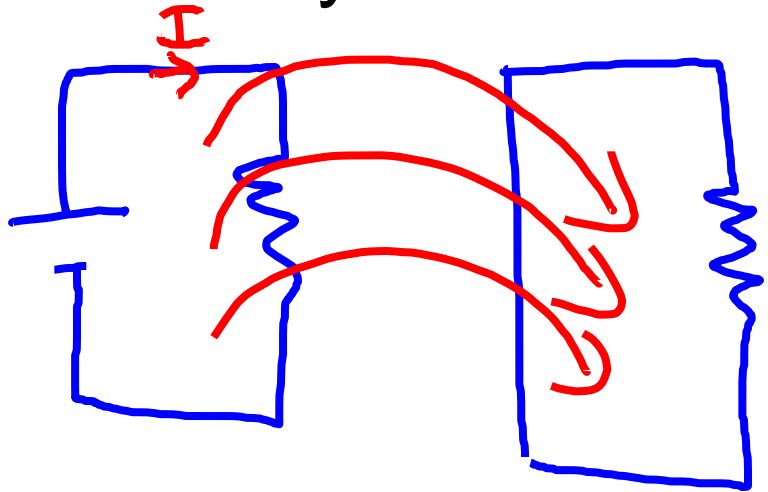
Faraday's Law

- A changing magnetic field induces a *curly* electric field – one for which you cannot define a potential V .

$$\mathcal{E} = \oint \vec{\mathbf{E}} \cdot d\vec{\mathbf{l}} = - \frac{d}{dt} \int \vec{\mathbf{B}} \cdot \hat{\mathbf{n}} dA$$

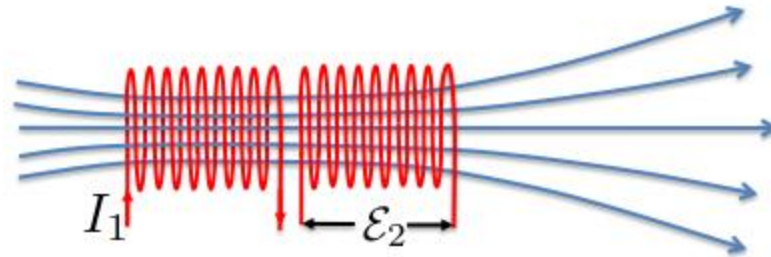
For the current in a stationary circuit to induce a current in an independent stationary circuit, it is necessary for the first circuit to have

- 1) a steady current.
- 2) a large current.
- 3) no current.
- 4) a changing current.
- 5) None of these is correct.



Mutual Inductance

- Emf will be induced in a coil when the flux through that coil is changing: $\mathcal{E} = -\frac{d}{dt} \int \vec{\mathbf{B}} \cdot \hat{\mathbf{n}} dA$
- That flux could be produced by current in a different coil: $B \propto I \Rightarrow \frac{dB}{dt} \propto \frac{dI}{dt}$
- So, a changing current in one coil, induces an emf in another coil: $\mathcal{E}_2 = M \frac{dI_1}{dt}$
- M = mutual inductance, a geometric and materials property.



Self Inductance

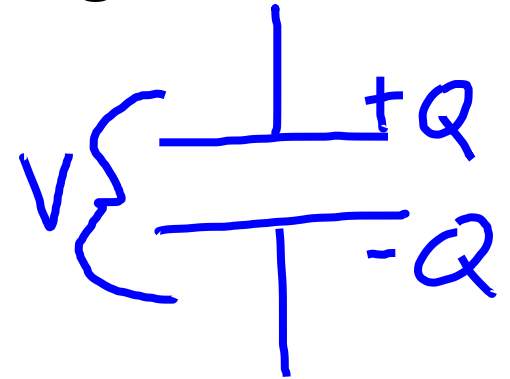
- A changing current in one part of a current-carrying circuit can induce an emf *in the same circuit*.

$$\varepsilon = -L \frac{dI}{dt}$$

- L = self inductance, a geometric and materials property.
- Units – Henry (H) = Vs/A = Ω s

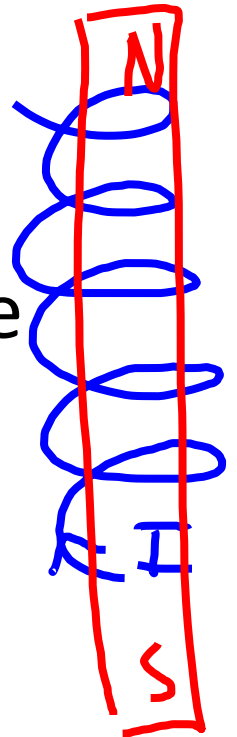
Capacitor

- Two conductors with opposite charges on them.
- Stores charge and energy.
- Capacitance:
 - Charge “moved” from one conductor to the other is proportional to the potential difference between the conductors. $Q = CV$
 - Capacitance is a geometric and materials property.



Inductor

- A current-carrying wire formed into some geometric shape (e.g. a solenoid).
- Stores magnetic flux and energy.
- Inductance:
 - Magnetic flux inside the inductor is proportional to the current passing through it: $N\Phi_B = LI$
 - Constant of proportionality L is called *inductance*.
 - Inductance is a geometric and materials property.



$$\mathcal{E} = -N \frac{d\Phi_B}{dt} = -\frac{d(LI)}{dt} = -L \frac{dI}{dt}$$

Solenoid

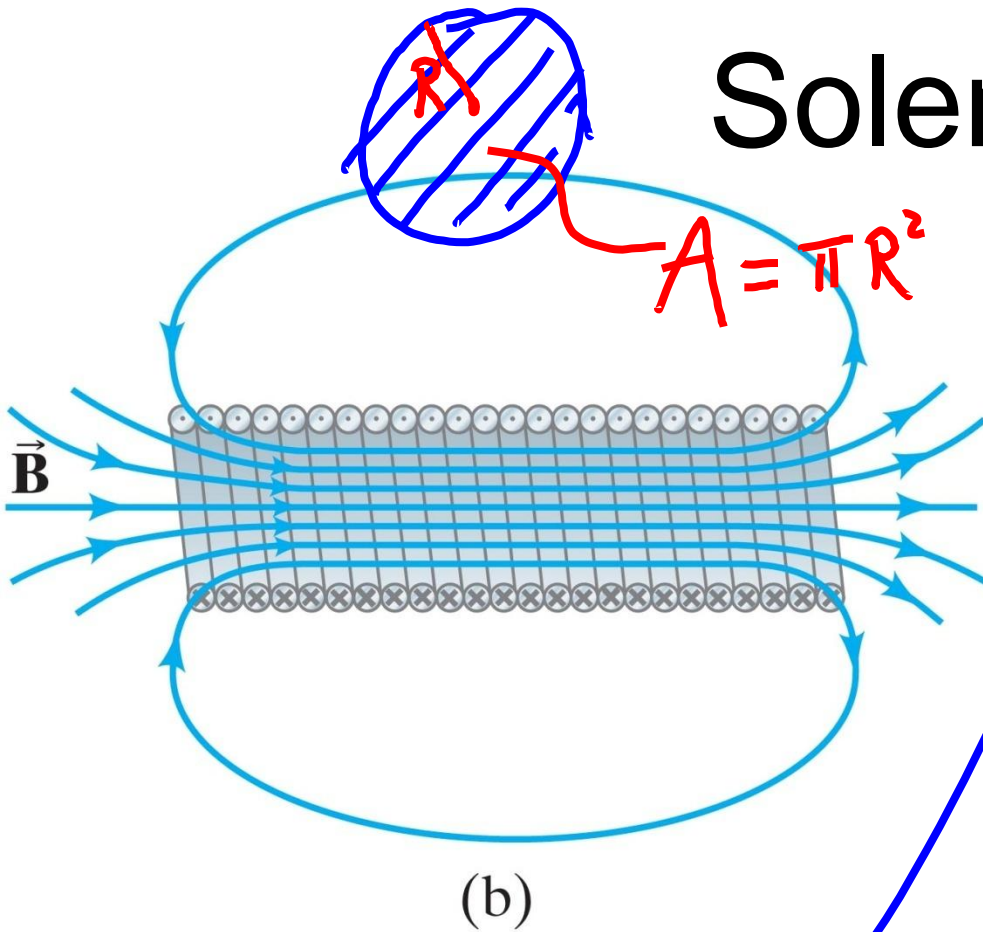


Figure 28.15b

$$B = \frac{\mu_0 NI}{l}$$

$$\Phi_B = BA = \frac{\mu_0 NIA}{l}$$

$$N\Phi_B = LI$$

$$\frac{N\mu_0 NIA}{l} = LI$$

$$L = \frac{\mu_0 N^2 A}{l}$$

A solenoid is constructed with N loops of wire tightly wrapped around an iron-filled center. Due to budget cuts, the current that ordinarily runs through this solenoid is cut in half. As a result, the inductance of the solenoid is

- 1) unchanged.
- 2) quartered.
- 3) halved.
- 4) doubled.
- 5) quadrupled.